

SCIENTIFIC MACHINE LEARNING GUIDED BY NUMERICAL ANALYSIS

YOUNGJOON HONG^{*} AND HWIJAE SON[†]

^{*} Seoul National University
1 Gwanak-ro, Gwanak-gu, Seoul 08826, Republic of Korea
hongyj@snu.ac.kr

[†] Konkuk University
120 Neungdong-ro, Gwangjin-gu, Seoul 05029, Republic of Korea
hwijaeson@konkuk.ac.kr

Key words: Machine Learning, AI, Scientific Computing, Numerical Analysis, Fluid Dynamics.

ABSTRACT

Scientific machine learning has rapidly emerged as a powerful paradigm for solving challenging problems in science and engineering, including partial differential equations, inverse problems, multiscale modeling, data assimilation, uncertainty quantification, and the discovery of governing laws from data. In particular, it is becoming increasingly important in applied mathematics and computational fluid dynamics, where one aims to model, simulate, and predict complex flow phenomena such as turbulence, multiphase flows, fluid–structure interaction, geophysical flows, and high-dimensional parametric fluid systems. Despite remarkable empirical success, many SciML methods still face fundamental challenges related to stability, accuracy, convergence, generalization, interpretability, and robustness, especially when available data are sparse, noisy, high-dimensional, or expensive to obtain.

The objective of this Minisymposium is to highlight the essential role of numerical analysis in developing reliable, efficient, and mathematically grounded scientific machine learning methods, with particular emphasis on applications to fluid mechanics and flow-related scientific computing. Classical concepts from numerical analysis, such as discretization, stability, convergence, structure preservation, error estimation, and efficient solvers, provide a natural framework for understanding and improving modern learning-based approaches to scientific computing. Rather than viewing machine learning as a replacement for traditional numerical methods, this Minisymposium emphasizes hybrid approaches in which data-driven models are guided, constrained, or enhanced by numerical principles and physical laws governing fluid flows. Topics of interest include physics-informed neural networks [1], neural operators [2], operator learning [3], reduced-order modeling [4], inverse problems, data assimilation, uncertainty quantification, turbulence modeling, flow control, and foundation models for scientific and fluid dynamical systems.

REFERENCES

- [1] M. Raissi, P. Perdikaris and G.E. Karniadakis, “Physics-informed neural networks: A deep learning framework for solving forward and inverse problems involving nonlinear partial differential equations”, *Journal of Computational Physics*, Vol. 378, pp. 686–707, 2019.
- [2] Z. Li, N. Kovachki, K. Azizzadenesheli, B. Liu, K. Bhattacharya, A. Stuart and A. Anandkumar, “Fourier Neural Operator for Parametric Partial Differential Equations”, *International Conference on Learning Representations*, 2021.
- [3] J.Y. Lee, S. Ko and Y. Hong, “Finite Element Operator Network for Solving Elliptic-Type Parametric PDEs”, *SIAM Journal on Scientific Computing*, 2025.
- [4] J. Choi, T. Yun, N. Kim and Y. Hong, “Spectral Operator Learning for Parametric PDEs Without Data Reliance”, *Computer Methods in Applied Mechanics and Engineering*, 2024.